Impacts of Polystyrene Molecular Weight and Modification to the Repeat Unit Structure on the Glass Transition—Nanoconfinement Effect and the Cooperativity Length Scale

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ABSTRACT: The effect of nanoconfinement on the glass transition temperature $(T_{\rm g})$ of supported polystyrene (PS) films is investigated over a broad molecular weight (MW) range of 5000–3 000 000 g/mol. Polystyrene MW is shown to have no significant impact on the film thickness dependence of $T_{\rm g}$ – $T_{\rm g,bulk}$. In contrast, a small modification to the repeat unit structure of PS has a dramatic impact on the $T_{\rm g}$ -nanoconfinement effect. The strength of the thickness dependence of $T_{\rm g}$ is greater for poly(4-methylstyrene) (P4MS) than for PS and yet much greater for poly(4-tert-butylstyrene) (PTBS). The $T_{\rm g}$ reduction for PTBS is 47 K below $T_{\rm g,bulk}$ for a 25 nm thick film, with the onset thickness for confinement effects in PTBS being 300–400 nm. Measurements of the size of cooperatively rearranging regions, $\xi_{\rm CRR}$, in bulk polymer systems at $T_{\rm g}$ reveal that PS MW has no significant effect on $\xi_{\rm CRR}$ unless PS is oligomeric or nearly oligomeric. However, changes to repeat unit structure and diluent addition affect $\xi_{\rm CRR}$ values, but not in a manner that yields an obvious correlation with the $T_{\rm g}$ -nanoconfinement effect.

Introduction

When confined to nanoscale dimension, both low molecular weight¹⁻⁶ and polymeric⁷⁻³⁶ glass formers have been widely observed to exhibit glass transition temperatures (T_{gS}) that deviate substantially from their bulk values. This behavior has implications in applications such as photoresists, disk drive lubricants, asymmetric membranes, and nanocomposites, among others. This broadly based technological impact and the strong dependence of many key material properties (mechanical, viscoelastic, diffusive, etc.) on the proximity of temperature to $T_{\rm g}$ have driven research efforts in this area. Thin and ultrathin films have dominated research into nanoconfined polymer behavior due to the ease with which the confining dimension, film thickness, can be varied. Polymer films may be supported by a substrate^{7-24,30-37} or freely standing (unsupported). ^{13,14,26-29} For freely standing films, $T_{\rm g}$ decreases with decreasing film thickness. In contrast, for supported polymer films, increases in $T_{\rm g}$ for polymers with strong attractive substrate interactions $^{8,9,14-16,22,23,35}$ and decreases in $T_{\rm g}$ for polymers with neutral or repulsive substrate interactions^{7,8,10–24,32,34–36} have been observed with decreasing thickness. In a few cases involving copolymers with comonomer units that exhibit attractive and neutral or repulsive substrate interactions, T_g has been observed to be nearly invariant with film thickness. 33,37 Various methods have been used to characterize T_g in polymer films, including dielectric relaxation spectroscopy, ^{12,30,31} fluorescence spectroscopy, ^{22–25} Brillouin scattering, ^{13,26–28} ellipsometry, ^{7,8,10,13,15–20,29,32–35} X-ray reflectivity, ^{9,21,35,36} and nonlinear optics. ³⁷

Many postulates have been offered regarding the origin of these effects¹⁴ in systems lacking attractive polymer—substrate interactions: internal stresses caused

by film preparation methods (e.g., spin-coating);^{38,39} a "finite size effect" due to the thickness approaching a fundamental length scale associated with glass formers, ⁷ e.g., the cooperatively rearranging region (CRR) introduced by Adam and Gibbs;⁴⁰ interfacial effects involving a reduced entanglement concentration 18,38,39,41 or a segregation of chain ends to the free surface (airpolymer interface); 18,42 and a radius of gyration $(R_{\rm g})$ that is on the order or a small multiple of the film thickness, $h.^{20,29}$ With supported polystyrene (PS) films, two reviews 10,14 have found extensive agreement for the $T_{
m g}$ nanoconfinement effect across many measurement methods: when scaled according to the bulk $T_{\rm g}$ as $T_{\rm g}(h)/T_{\rm g,bulk}$, 43 the thickness dependence of $T_{\rm g}$ has been found to be approximately independent of PS molecular weight $(MW)^{10-12,14,18}$ over a \overline{MW} range of 3600-2900000g/mol.

The notion that internal stresses cause the $T_{\rm g}$ -nanoconfinement effect may be refuted by the agreement among many studies of supported PS films 10,14 in which films of similar thickness were prepared using different solutions (solvent type and polymer concentration) and preparation conditions (spin-coating speed). However, related studies of ultrathin PS^{44,45} and polycarbonate⁴⁶ films have shown the existence of a negative thermal expansivity in the glassy state which has been attributed to a nonrelaxed structure that is set in during spin-coating. 21,44 This effect, which exhibits little impact on $T_{\rm g}$, 44 can be removed by annealing at $T_{\rm g,bulk} + 50$ K for 2 h. 21,44

There has been interest 14 in connecting the size scale at which nanoconfinement effects are observed to the size scale of a CRR. (Adam and Gibbs 40 introduced the concept of a CRR in which local relaxation occurs by the collective motion of many molecules or polymer segments.) The length scale of a CRR near $T_{\rm g}$ has been investigated by differential scanning calorimetry, $^{47-52}$ 4D NMR, 53,54 and other techniques 55,56 and has been reported to lie in the range of $\sim \! 1\!-\!4$ nm for low MW and polymeric glass formers. However, the length scale

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at which nanoconfinement effects are observed is $\sim \! 10$ nm or less for low MW glass formers^{1–6} and ranges from several tens to more than one hundred nanometers for polymers.^{7–37} This indicates that the length scale of a single CRR is far less than the thickness at which $T_{\rm g}$ -nanoconfinement effects are observed.

Recent understanding gained from fluorescence experiments 24 has reiterated this point. These experiments have revealed via multilayer PS films with fluorescent labels in only one layer that the free surface effect causes a $T_{\rm g}$ reduction that persists several tens of nanometers into the film interior (much larger than a single CRR). Furthermore, it was observed that a region of reduced $T_{\rm g}$ near the free surface exists as a continuous distribution of $T_{\rm g}$ s that depends on the degree of nanoconfinement. These results have shown directly that two-layer and three-layer models $^{9-12,14,27}$ are inadequate to explain $T_{\rm g}$ -nanoconfinement behavior and that a model that incorporates a continuous distribution of $T_{\rm g}$ s across the thickness of a film is needed. This picture is consistent with recent simulations 57 and predictions from theoretical pictures.

Many other studies $^{6,8,14,17,60-64}$ have indicated that interfacial effects are the most logical explanation for the underlying cause of the $T_{\rm g}$ -nanoconfinement effect. Numerous studies have concluded $^{24,57-64}$ that the freesurface $T_{\rm g}$ of bulk PS films is some tens of degrees lower than the bulk $T_{\rm g}$. Supporting the importance of freesurface effects for PS, a recent study 17 has shown that removing the free-surface interface by placement of Al or Au metal onto the film results in a $T_{\rm g}$ that is independent of thickness down to 10 nm or less. The key role of interfacial effects is also supported by studies of the thickness dependence of $T_{\rm g}$ for polymers with attractive substrate interactions, 8,9,15,16,22,23,33 e.g., poly-(2-vinylpyridine) and poly(methyl methacrylate) on silicon (with native oxide) or glass substrates which exhibit increases in $T_{\rm g}$ with decreasing thickness due to the attractive substrate interactions.

Although there is substantial evidence supporting a free-surface effect as the origin of $T_{\rm g}$ reductions in nanoconfined PS films, there is not yet a detailed understanding of the free-surface effect. A simple explanation is that polymer segments that lie at the free surface possess fewer conformational restrictions than those in the bulk and thus have a higher degree of cooperative segmental mobility and an associated lower $T_{\rm g}$. While this explanation is logical, it lacks details regarding the extent to which interfaces may be expected to modify cooperative segmental mobility or $T_{\rm g}$ from that of bulk. Others have offered the explanation that the free surface results in a reduced entanglement concentration, 18,38,39,41 which in turn yields enhanced mobility and reduced T_g near the free surface. However, this explanation can be criticized because a thicknessdependent $T_{\rm g}$ has been observed for both entangled and unentangled $PS^{10-12,14,18}$ (M_c , the critical entanglement MW, is \sim 35 000–38 000 g/mol 65,66 for PS) and because bulk $T_{\rm g}$ does not depend on chain entanglements.⁶⁵

Another potential explanation involves the segregation of chain ends to the free surface that would be expected to reduce the local $T_{\rm g}$ at the free surface. ^{18,42} However, if chain ends were the origin of this effect, it would be expected that the thickness dependence of $T_{\rm g}$ could be significantly altered by varying the surface chain-end concentration by modification of the polymer MW, ⁴² which is not supported by experimental data.

Variation of polymer MW also greatly alters the $R_{\rm g}$ of the bulk polymer, which in turn would significantly affect the film thickness at which overall chain conformation would be expected to differ substantially from bulk. For example, when PS MW is increased from 3600 to 2 900 000 g/mol, the bulk $R_{\rm g}$ increases from $\sim\!2$ to 47 nm (using a characteristic ratio of 10 to calculate $R_{\rm g}^{65,67}$).68 Some have argued that such an effect may yield a MW dependence of the $T_{\rm g}$ -nanoconfinement effect. 20,30 In opposition to this picture is a large body of evidence $^{10-12,14,18}$ indicating that the $T_{\rm g}$ -nanoconfinement effect for supported PS films is approximately independent of MW; this means that neither chain ends nor bulk $R_{\rm g}$ plays a significant role in defining this effect.

It is noteworthy that two very recent studies 20,21 of supported PS films have reported a MW dependence of the $T_{\rm g}$ -nanoconfinement effect in the range of 212 000—2 900 000 g/mol. 69 Singh et al. 20 reported that the thickness dependence of $T_{\rm g}$ for a variety of PS MWs can be collapsed onto a master curve when thickness is scaled as $h/R_{\rm g}$ (bulk) and $T_{\rm g}$ is scaled as $T_{\rm g}(h)/T_{\rm g,bulk}$. While the study by Miyazaki et al. 21 was largely focused on thermal expansion effects, it also reported a larger $T_{\rm g}$ -nanoconfinement in ultrathin films of higher MW (2 890 000 vs 303 000 g/mol) PS down to \sim 10 nm in thickness.

As a result of this recent disagreement regarding the impact of MW on the $T_{\rm g}$ -nanoconfinement effect in supported PS films as well as the results of our study showing that this effect can be dramatically reduced by addition of low MW diluents, we have chosen to study the tunability of the $T_{\rm g}$ -nanoconfinement effect by making small changes to the molecular structure of PS. We have also investigated the effects of these changes in molecular structure on the cooperativity length scale at $T_{\rm g}$. The changes in structure include the largest range of MWs examined to date in a single study of supported PS films as well as modifications to the repeat unit involving a comparison of PS to P4MS and PTBS, all supported on glass substrates.

Experimental Section

Polystyrene standards were purchased from Polysciences Inc. and Pressure Chemical Co. and used as received. Samples of PS films with $M_{\rm n} = 5000$ g/mol were prepared by codissolving a high MW PS standard ($M_n = 200\,000\,\text{g/mol}$) with a low MW PS standard ($M_n = 1850$ g/mol) in toluene (99.9% purity) prior to film preparation. Pyrene-labeled PS was synthesized by copolymerizing a 1-pyrenylbutyl methacrylate with styrene, resulting in a polymer with 1 in 170 repeat units being a pyrene-labeled methacrylate; details of the synthesis are reported elsewhere. ²⁴ Poly(4-methylstyrene) (P4MS) was from Scientific Polymer Products and used as received. Poly(4-tertbutylstyrene) (PTBS), poly(vinyl acetate) (PVAc), and glycerol (99.5+%) were from Aldrich. Because of the presence of 4-tertbutylstyrene monomer in the as-received polymer, the PTBS sample was dissolved in toluene (99.9% purity) and precipitated seven times in methanol (99.9% purity) to ensure monomer removal prior to use. $T_{\rm g,bulk}$ values were measured as $T_{\rm g,onset}$ values by differential scanning calorimetry (DSC) (Mettler Toledo DSC822) on second heat at 10 K/min. Polymer MW was determined by gel permeation chromatography (GPC) (Waters) relative to a PS calibration unless otherwise noted. Table 1 provides details on values of sample M_n , M_w/M_n , and $T_{
m g,bulk}$ by DSC and $T_{
m g,bulk}$ as determined by this fluorescence method. Pyrene (Aldrich Chemical, 99+% purity), 1,10-bis(1pyrene)decane (BPD) (Molecular Probes), and dioctyl phthalate (DOP) (Aldrich, 99%) were used as received.

Table 1. Molecular Weight and Bulk T_g for Materials **Employed in This Study**

material	$M_{ m n}$ (g/mol)	$M_{ m w}\!/\!M_{ m n}$	$T_{ m g,bulk} \left({ m K} ight) \ \left({ m onset, DSC} ight)$	$T_{ m g,bulk}\left(m K ight) \ m (fluor)$
PS	23000000	1.30	374	
PS	3000000	1.05	374	373
PS	400000	1.06	375	
PS	263000	1.10	373	373
PS	200000	1.08	373	373
PS	13500	1.06	368	
PS	12000	1.10	365	364
PS	5000	$\operatorname{bimodal}^a$	358	358
PS	1850	1.14	333	
PS	800	1.11	269	
PS	568	1.13	248	
P4MS	279000	1.57	376	376
PTBS	32000	3.31	404	404
PS w/pyrene label	440000	1.73	369	371
glycerol			188	

^a Blend of 1850 and 200000 g/mol PS.

Thin films were prepared by spin-coating 70 dilute solutions of polymer in toluene (Fisher, used as received) onto glass slides. The slides were initially washed with a 10% sodium hydroxide/70% ethanol/20% water solution²² and then solvent washed between experiments. Film thickness was measured with a Tencor P10 profilometer. Calibration of the profilometer was verified using a 14 nm step-height standard (VLSI standards). At least 10 measurements were taken in total at different locations close to the center of the film (where fluorescence was measured) and averaged with the typical standard deviation in these measurements being less than 1.5 nm for films thicker than ~20 nm and ~1.0 nm for films thinner than \sim 20 nm.

A Spex Fluorolog-2DM1B fluorimeter was used for steadystate fluorescence measurements. Measurements employed front-faced geometry with 2.5 mm excitation and emission slits (band-pass = 4.5 nm) for films with thickness < 100 nm and 1.25 mm excitation and emission slits (band-pass = 2.25 nm) for films with thickness > 100 nm. In the worst case, the signal-to-noise ratio exceeded 30. The probe (pyrene or BPD) content in each film was <0.2 wt % of dry polymer content. (At this probe concentration the $T_{\rm g}$ value of pyrene-doped polymer is the same within error as that of neat polymer, a circumstance that also holds for BPD.) A clean quartz cover slide was placed on top of each film to reduce the potential for probe sublimation during the $T_{\rm g}$ measurement by fluorescence. (The film was adhered only to the glass substrate on which it was spin-coated.) Film temperature was controlled by a microprocessor controller (Minco Products) with a Kapton ribbon heater attached to a flat aluminum plate that was also used as a clamping device to hold the sample. The excitation wavelength was 322 nm for all samples, and the emission spectrum was measured at 350-450 nm. No excimer fluorescence was observed in any sample. Fluorescence spectra were recorded upon cooling after having annealed samples at $\sim T_{\rm g}$ + 40 K for 15 min. In the case of the PS with $M_{\rm n}=3\,000\,000$ g/mol, samples were annealed at $\sim T_{\rm g}$ + 40 K for 45 min; in the case of PS with $M_{\rm n} \leq 12~000$ g/mol, dewetting problems were reduced or eliminated by annealing for 15 min at $\sim T_{
m g}$ + 35 K.

In fitting the temperature dependence of fluorescence in the rubbery and glassy states, only data points well outside T_{σ} were used for the linear fits, and typical correlation coefficients (R^2) were better than 0.990. To initiate the fitting procedure, data points were added to the rubbery- and glassy-state linear regressions at the extrema in the temperature range of the data. The correlation coefficient was monitored as more data points were added (approaching $T_{\rm g}$ from the extrema in the temperature range of the data) to each of the linear regressions. If the R^2 value began to steadily decrease below a threshold value (i.e., <0.990) as more data points were added, then these data points were removed to produce a value of R^2

higher than the threshold value, and the linear regressions were considered acceptable. The linear fits in both the rubbery and glassy states included a minimum of four fluorescence data points (usually more), spanning a minimum of 15 K in temperature. This procedure was followed regardless of whether fitting linear functions to the fluorescence intensity data at particular emission wavelength(s) or the integrated intensity as a function of temperature. When using integrated intensities to identify $T_{\rm g}$ (the usual case), spectra were taken over a sufficient range of wavelengths that integration could be done from instrument baseline at the lowest wavelengths to the same instrument baseline at the highest wavelengths.

When fitting the temperature dependence of the fluorescence intensity data at the peaks in the emission spectra (as done previously in refs 22-25), the standard deviation in the determination of $T_{\rm g}$ at the various peaks in the emission spectra was typically less than 1.0 K for each sample. This is comparable to the estimated standard variation (or error) in $T_{\rm g}$ (± 1.0 K or less) from sample to sample (identified either using intensities or integrated intensities) for films of identical thickness on identical substrates when the film thickness is greater than \sim 25 nm. As film thickness decreased below \sim 25 nm, the estimated standard variation (or error) is estimated to be ± 2 K. Further details on measurement of $T_{\rm g}$ by fluorescence are given elsewhere. $^{22-25}$

Differential scanning calorimetry (Mettler Toledo DSC822) was used to measure the heat capacity for the determination of the size of the CRR. 47,48 Initially, the furnace was heated to 973 K in the presence of oxygen to oxidize any impurity present from previous use. Specific heat capacities were measured against a sapphire standard. A blank pan was run followed by a sapphire standard immediately prior to characterization of each polymer sample. The calibration of the DSC instrument was regularly monitored via an indium standard. All DSC measurements were taken on the second heating (10 K/min) cycle after quenching (40 K/min) from elevated temperature. Samples were annealed for at least 45 min at the elevated temperature (353 K for PS $M_{\rm n} = 800$ g/mol and PS $M_{\rm n} = 568$ g/mol and 473 K for the other samples) before quenching to erase prior thermal history and, even more importantly, to optimize sample-pan contact. All thermograms used in heat capacity measurements and thereby the determination of the size of the CRR were taken from $T_{
m g,bulk}-70$ K to $T_{
m g,bulk}+70$ K in order to measure baselines accurately. The reported heat capacity values are averages of a minimum of six runs. Further details are available in the Supporting Information for this paper.

Results and Discussion

Comparison of T_{g} -Nanoconfinement Effects as a Function of PS MW. Figure 1a shows the fluorescence emission spectrum of pyrene dopant in an 810 nm thick PS film. There is a significant reduction in overall intensity with increasing temperature (T). Previous studies have shown^{22–25} that $T_{\rm g}$ values can be obtained by plotting the intensity near one or several of the peak wavelengths (~374, 385, and 395 nm) as a function of T. Over a 70-80 K T range roughly centered at T_g , two linear T dependences of intensity are observed, a stronger one in the rubbery state and a weaker one in the glassy state, with the intersection being identified as $T_{\rm g}$. Careful inspection of Figure 1a reveals that the exact values of the two slopes in such a plot may depend on the emission wavelength selected because the T dependence of intensity is stronger at the maxima (peaks) than at the minima (valleys) of the emission spectrum. Such effects have been observed by others^{71,72} studying the T dependence of pyrene fluorescence in various polymers and can be attributed to the T dependence of the different vibronic bands of pyrene. In addition to these effects, there are slight blue shifts in the emission spectrum of pyrene (1-2 nm) as T is

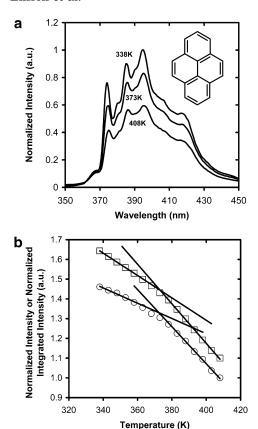


Figure 1. (a) Fluorescence emission spectra of pyrene dopant (<0.2 wt %) in an 810 nm thick PS ($M_{\rm n}=200~000~{\rm g/mol}$) film taken at 338, 373, and 408 K. The inset shows the structure of pyrene. (b) T dependence of the fluorescence intensity (\bigcirc) monitored at an emission wavelength of 400 nm and integrated intensity (\square) of pyrene dopant in an 810 nm thick PS film ($M_{\rm n}=200~000~{\rm g/mol},~T_{\rm g,bulk}=373~{\rm K}$). (The intensity and integrated intensity have been normalized to one at 408 K and arbitrarily shifted.)

decreased from 413 to 333 K. To minimize these effects, we have chosen to plot values of integrated intensity as a function of T. Figure 1b compares the T dependence of integrated intensity to that of intensity at 400 nm; while the same $T_{\rm g}$ value (373 K) is determined from both plots, there is a discernible difference in the T dependences of intensity at 400 nm and the integrated intensity over a common T range.

Figure 2a shows the T dependence of integrated intensity for PS with $M_{\rm n}=5000$ g/mol at two thicknesses (500 and 29 nm, $T_{\rm g}=356$ and 344 K, respectively). Similarly, Figure 2b shows a higher MW PS with $M_{\rm n}=200~000$ g/mol at two thicknesses (24 and 810 nm, $T_{\rm g}=358$ and 373 K, respectively). In accord with earlier fluorescence studies $^{22-25}$ of the $T_{\rm g}$ -nanoconfinement effect as well as other studies, 10 these figures demonstrate a weakening in the strength of $T_{\rm g}$ in highly nanoconfined PS films. In the studies conducted here, a weakening in the strength of $T_{\rm g}$ for PS is observed with decreasing thickness for films less than ~ 30 nm thick, independent of PS MW. Associated with this strength of $T_{\rm g}$ effect, the error in estimating $T_{\rm g}$ values by the intersection of linear temperature dependences of integrated intensity in the rubbery and glassy states is $\sim \pm 1$ K when film thickness is greater than $\sim 20-25$ nm and $\sim \pm 2$ K when film thickness is less than ~ 20

Figure 3 shows the thickness dependence of T_g for PS M_n values ranging from 5000 to 3 000 000 g/mol, which

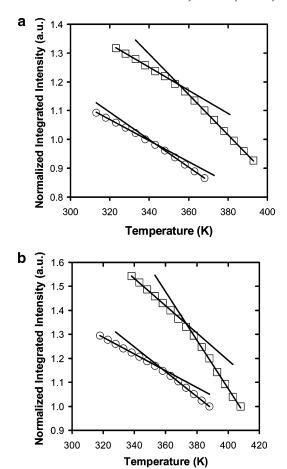


Figure 2. (a) *T* dependence of the integrated intensity of pyrene dopant in 500 nm thick (□) and 29 nm thick (○) PS ($M_{\rm n}=5000~{\rm g/mol},~T_{\rm g,bulk}=358~{\rm K}$) films. (The integrated intensity has been normalized to one at 368 and 338 K, respectively, and arbitrarily shifted.) (b) T dependence of the integrated intensity of pyrene dopant in 810 nm thick (□) and 24 nm thick (□) PS ($M_{\rm n}=200~000~{\rm g/mol},~T_{\rm g,bulk}=373~{\rm K}$) films. (The integrated intensity has been normalized to one at 408 and 388 K, respectively, and arbitrarily shifted.)

is the broadest range in MWs ever examined in a single $T_{\rm g}$ -nanoconfinement study. The data in Figure 3 indicate that there is no significant MW dependence over a broad range in PS MWs within the error of these measurements. The solid curve in Figure 3 represents a fit of all the PS data to the relation $T_g(h) = T_{g,\text{bulk}}(1 - 1)$ $(A/h)^{\delta}$) originally proposed by Keddie et al. with A =3.2 nm and $\delta = 1.63$. (The apparent differences in the data for the thinnest films of the 5000 and 3 000 000 g/mol samples should not be taken as significant. There is a ± 1 nm uncertainty associated with those film thicknesses, and in the thinnest films this level of uncertainty has a very substantial effect in the extent of the $T_{\rm g}$ reduction relative to $T_{\rm g,bulk}$. That factor, combined with the ± 2 K uncertainty in assigning the $T_{\rm g}$ value in films less than 20 nm in thickness, is sufficient to indicate that any apparent difference of the $T_{\rm g}$ -nanoconfinement effect as a function of PS MW is not significant, given the inherent quality of the data.)

This demonstration of the independence of the $T_{\rm g}$ -nanoconfinement effect with respect to MW in supported PS films is consistent with many previous reports^{10–12,14,18} covering a $M_{\rm n}$ range of 3600–2 900 000 g/mol but is in contradiction with two very recent studies^{20,21} that have reported some MW dependence in the range of 212 000–2 900 000 g/mol. It is noteworthy that these two very

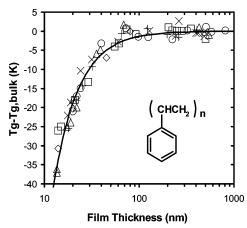


Figure 3. $T_{\rm g}-T_{\rm g,bulk}$ as a function of film thickness for PS $[M_{\rm n}=5000~{\rm g/mol}~(\Box),\,M_{\rm n}=12~000~{\rm g/mol}~(+),\,M_{\rm n}=200~000$ g/mol (\bigcirc), $M_{\rm n}=263~000$ g/mol (\times) (reported previously in refs 22–25), $M_{\rm n}=3~000~000$ g/mol (\diamondsuit)] films as measured by pyrene dopant fluorescence and PS $[M_n = 440\ 000\ g/mol\ (\triangle)]$ as measured by pyrene label fluorescence (reported previously in ref 24). The curve represents a least-squares fit of the data to the empirical relation originally proposed by Keddie et al., yielding parameter values A = 3.2 nm and $\delta = 1.63$. The inset shows the structure of the PS repeat unit.

recent studies are in some disagreement regarding how PS MW impacts the $T_{\rm g}$ -nanoconfinement effect. For example, Singh et al.²⁰ reported a $T_{\rm g}$ for 100 nm thick films that is 3 K lower for 1 600 000 g/mol PS than for 560 000 g/mol PS with a maximum difference of \sim 4 K between $T_{\rm g}$ values among PS MWs at any particular thickness. In contrast, Miyazaki et al. 21 reported no $T_{
m g}$ difference (within error) between 303 000 and 2 890 000 g/mol PS in 100 nm thick films but about a 7 K maximum difference for 20 nm thick films. (Some of the $T_{\rm g}$ data from Miyazaki et al.²¹ have large error bars, bringing into question the extent to which there is a true statistical difference in nanoconfined $T_{\rm g}$ values as a function of MW.)

At present, the cause for the disagreement between the many studies, including the present one, indicating that there is no significant MW dependence of the $T_{\rm g}$ nanoconfinement effect in supported PS films and the two other recent studies indicating the opposite is not known. However, it is noteworthy that Fukao and coworkers^{12,30} had concluded in 1999 and 2000 that there was some MW dependence to the $T_{
m g}$ -nanoconfinement effect in supported PS films but later concluded³¹ in 2002 that there was no MW dependence, which may be an indication of the difficulty in obtaining the highest quality data from what may be deceptively simple studies. A factor that may contribute to the different results obtained by Singh et al.²⁰ and by Miyazaki et al.²¹ is that their studies reported $T_{\rm g}$ data taken upon heating from the glassy state after a 10 K/10 min stepand-hold method^{20,21} while most other studies, including the present one, have been taken upon cooling from the rubbery state. Measuring $T_{\rm g}$ upon cooling eliminates issues regarding how physical aging, which itself may be a function of thickness in nanoconfined films, 22,73,74 affects the measured $T_{\rm g}$. In any case, we believe that the excellent agreement reported in Figure 3 among the many samples with M_n values over a broader range than in any previous single study provides ample evidence of the lack of a significant MW dependence to the $T_{\rm g}$ nanoconfinement effect in supported PS films. As such, these results provide further evidence that neither a

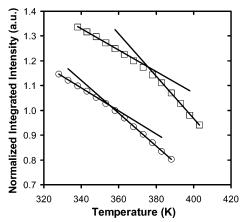


Figure 4. T dependence of the integrated intensity of pyrene dopant in 810 nm thick (□) and 24 nm thick (○) P4MS films $(T_{\rm g,bulk} = 376 \text{ K})$ films. (The integrated intensity has been normalized to one at 368 and 358 K, respectively, and arbitrarily shifted.)

reduction in entanglement concentration with a reduction in film thickness nor a modification of $R_{\rm g}$ upon confinement plays a significant role in the thickness dependence of $T_{\rm g}$. Furthermore, the fact that the results obtained with the PS sample with $M_{\rm n}=5000$ g/mol, made from a blend of high and very low MW PS standards, agree with those of many nearly monodisperse PS standards effectively demonstrates that chain end segregation plays no significant role in the $T_{\rm g}$ nanoconfinement effect. (It should be noted that the concentration of chain ends in a bulk system is only dependent on M_n . However, in a film made of a blend of very low MW and high MW polymer, it is possible⁴² that the very low MW PS will segregate to the free surface or air-polymer interface, thereby dramatically increasing the chain end concentration near the surface beyond that expected in a monodisperse system with identical $M_{\rm n}$.)

B. Comparison of T_g -Nanoconfinement Effects as a Function of Repeat Unit Structure. In contrast to the independence of the $T_{\rm g}$ -nanoconfinement effect to PS MW reported in section A, in this section we demonstrate that modifications to the repeat unit structure can significantly impact the $T_{\rm g}$ -nanoconfinement effect in styrene-based polymers. In particular, P4MS and PTBS systems are compared with PS.

Figure 4 shows the T dependence of the integrated intensity for pyrene-doped P4MS at two thicknesses. Similar to the PS case, P4MS shows a reduced strength in $T_{\rm g}$ in highly nanoconfined films. (As with PS, a weakening in the strength of T_g for P4MS is observed with decreasing thickness for films less than ~30 nm thick.) The 24 nm thick and 810 nm thick P4MS films display $T_{\rm g}$ s of ~ 355 and 376 K, respectively. In the case of films of thickness less than 25 nm, the estimated error in $T_{\rm g}$ is ${\sim}\pm2$ K while for thicker films it is ${\sim}\pm1$

Figure 5 shows the thickness dependence of $T_{\rm g}$ for P4MS compared to the PS data fit to the empirical function from Keddie et al.⁷ as shown in Figure 3. For 24 nm thick films, P4MS exhibits a $T_{\rm g}$ value that is reduced by 21 K relative to $T_{\rm g,bulk}$ while PS exhibits a $T_{\rm g}$ value that is reduced by \sim 14 K relative to $T_{\rm g,bulk}$. This indicates that the addition of one methyl unit on the 4-position of the phenyl ring in the PS repeat unit can have a significant effect on the thickness dependence of $T_{\rm g}$. However, it is interesting to note that the onset

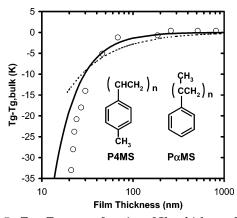


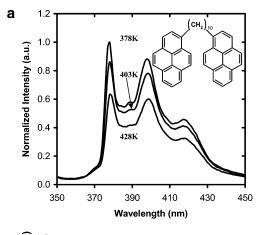
Figure 5. $T_{\rm g}-T_{\rm g,bulk}$ as a function of film thickness for P4MS (O) films as measured by pyrene dopant fluorescence. The bold curve represents a least-squares fit of the PS data (refer to Figure 3) to the empirical relation of Keddie et al.⁷ with parameter values A=3.2 nm and $\delta=1.63$; the dotted curve is a reproduction of the curve reported in a study of P α MS $T_{\rm g}$ -nanoconfinement effects (ref 19). The inset shows the P4MS and P α MS repeat unit structures.

thickness at which $T_{\rm g}$ begins to show a significant deviation from $T_{\rm g,bulk}$, which we define to be a 3 K reduction relative to $T_{\rm g,bulk}$, is virtually the same (\sim 45–50 nm) for P4MS and PS.

Kim et al. ¹⁹ have reported on the $T_{\rm g}$ -nanoconfinement effect observed in poly(α -methylstyrene) (P α MS), in which a methyl unit is located on the α -carbon along the chain backbone. Their data indicate that the onset thickness of the $T_{\rm g}$ reduction is greater (\sim 90–95 nm) for P α MS than for PS or P4MS. In addition, the shape of the thickness dependence of $T_{\rm g}$ for P α MS differs from that of PS or P4MS, decreasing much less steeply at thicknesses less than 40 nm. In agreement with our PS results, Kim et al. ¹⁹ reported no effect of MW on the reduction of $T_{\rm g}$ as a function of thickness for P α MS with MWs of 23 000 and 450 000 g/mol.

We have also used fluorescence to measure the T_g nanoconfinement effect in PTBS, which differs from the repeat unit structure of PS by the addition of a tertbutyl group to the 4-carbon on the phenyl ring. The addition of the tert-butyl group reduces the bulk density of the polymer by 10% compared to PS (from 1.04 to 0.94 g/cm³) and increases bulk $T_{\rm g}$ from $\sim \! 373$ to 404 K. In contrast, the densities and $T_{\rm g}$ values of P4MS and PS are nearly identical. This decreased density in PTBS may be attributed to significantly hindered packing of the repeat units of PTBS relative to PS which results in an increased free volume. Likely associated with these differences, we have observed that pyrene dopant is particularly susceptible to sublimation from PTBS films during annealing of the film above $T_{\rm g}$. To avoid sublimation issues, BPD, shown as the inset in Figure 6a, was chosen as a fluorescence dopant as it has diffusion coefficient in polymers near $T_{\rm g}$ that is several orders of magnitude lower than that of pyrene. 75 Various tests in PTBS indicated that BPD exhibits relatively little sublimation in the T range of interest.

Figure 6a shows the T dependence of the fluorescence emission spectra for BPD doped at trace levels (<0.2 wt %) into a 1190 nm thick PTBS film. The BPD dopant spectral shape is roughly similar to that of pyrene dopant in PS, with emission peaks at $\sim\!378$, 398, and 418 nm. Figure 6b shows the T dependence of the integrated intensities for two BPD-doped PTBS films; the 1190 nm thick film exhibits a $T_{\rm g}$ value of 404 K,



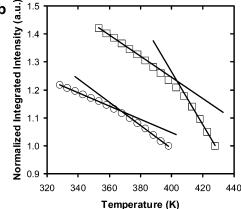


Figure 6. (a) Fluorescence emission spectra of BPD dopant in a 1190 nm thick PTBS film taken at 378, 403, and 428 K. The inset shows the structure of BPD. (b) T dependence of the integrated intensity of BPD dopant in 1190 nm thick (\square) and 30 nm thick (\square) PTBS ($T_{\rm g,bulk} = 404$ K) films. (The integrated intensity has been normalized to one at 428 and 398 K, respectively, and arbitrarily shifted).

equal to $T_{\rm g,bulk}$, while the 30 nm thick film exhibits a $T_{\rm g}$ of 368 K. The 30 nm thick PTBS film also shows a reduction in the strength of $T_{\rm g}$ compared to the 1190 nm thick film, qualitatively consistent with that shown for PS in Figures 2a,b and P4MS shown in Figure 4. (A weakening in the strength of $T_{\rm g}$ for PTBS is observed with decreasing thickness for films less than $\sim 30-35$ nm thick. The estimated error in the determination of $T_{\rm g}$ is ± 1 K for films with thickness exceeding 30 nm and ± 2 K for thinner films.)

Figure 7 compares the thickness dependence of T_g for PTBS and the dependences for P4MS and PS. Also shown are the $T_{\rm g}$ values of two 200 000 g/mol PS films doped with BPD, showing that BPD and pyrene dopant measure a consistent thickness dependence of $T_{\rm g}$ in PS. Figure 7 makes clear that there are dramatic differences in the $T_{\rm g}$ -nanoconfinement effect of PTBS as compared to that of either PS or P4MS. First, the onset thickness for $T_{\rm g}$ reduction in PTBS, estimated from Figure 7 to be 300-400 nm, is much larger than in PS or P4MS. (Strikingly, this value of onset thickness indicates that the effect is not necessarily limited to the "nano" length scale, often taken as 100 nm or less.) To the best of our knowledge, this is the largest thickness at which the T_g-nanoconfinement effect has ever been observed in supported or unsupported polymer films. In addition, the 47 K reduction in $T_{\rm g}$ relative to $T_{\rm g,bulk}$ observed in the 25 nm thick PTBS film is the largest $T_{\rm g}$ reduction observed experimentally in supported polymer films.

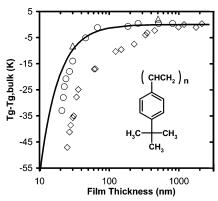


Figure 7. $T_{\rm g} - T_{\rm g,bulk}$ as a function of film thickness for P4MS (\bigcirc) films as measured by pyrene dopant fluorescence, PTBS (\diamondsuit) films as measured by BPD dopant fluorescence, and PS (\triangle) $(M_{\rm n}=200~000~{\rm g/mol})$ films as measured by BPD dopant fluorescence. The bold curve represents a fit of the PS data in Figure 3 to the empirical relation of Keddie et al. The inset shows the structure of the PTBS repeat unit.

This strongly enhanced thickness dependence of $T_{\rm g}$ in PTBS relative to PS and even P4MS demonstrates that there is substantial tunability of the T_g -nanoconfinement effect. These results complement those of ref 25 that first revealed a tunability of the $T_{\rm g}$ -nanoconfinement effect by the addition of low MW plasticizers, albeit in the opposite direction; i.e., the thickness dependence was reduced or eliminated upon diluent addition. Given the invariance demonstrated in the $T_{\rm g}$ nanoconfinement effect as a function of PS MW (from 5000 to 3 000 000 g/mol), such dramatic differences in the impact of confinement on PTBS relative to PS may be considered surprising. However, as the addition of the tert-butyl group to PS reduces the bulk density substantially (nearly to that of styrene monomer, which has a density of 0.90 g/cm³) while resulting in a more rigid chain due to steric effects, it may be unreasonable to expect that there should much similarity in the $T_{
m g}$ nanoconfinement in PS and PTBS, except for the fact that the $T_{\rm g}$ values are expected to decrease with decreasing thickness below some onset thickness.

Up to the present time, these factors of overall density and chain stiffness have not been described in the literature as being associated with $T_{\rm g}$ -confinement effects. Here we hypothesize that it is chain stiffness rather than polymer density that may be responsible for or at least is associated with the much more dramatic $T_{\rm g}$ -nanoconfinement effect in PTBS as compared to PS and P4MS. This hypothesis is supported by a the fact that a recent study⁷⁶ reported that polycarbonate, which has significantly greater chain stiffness than PS, exhibits a substantial $T_{\rm g}$ reduction relative to $T_{\rm g,bulk}$ at a thickness of 142 nm, far greater than that observed for PS or P4MS. Obviously, while interesting issues remain to be explored in this field with PS, it may be possible that much greater insight may be gained by undertaking other studies involving small changes in repeat unit structure like those employed in the present study or in determining the effect of film thickness on $T_{\rm g}$ on polymers that bear little resemblance to PS and that may be accompanied by major changes in chain stiffness, density, etc. Such studies are currently underway in our laboratory.

C. Comparison of the Length Scale of Cooperative Dynamics for PS as a Function of MW and Repeat Unit Structure to the $T_{\rm g}$ -Nanoconfinement Behavior. In a recent study that discussed the deter-

mination of the distribution of T_g values in nanoconfined PS,²⁴ it was shown that the free-surface effect results in a significantly reduced local $T_{\rm g}$ (by some tens of degrees) at the free surface and that the local T_g is perturbed from its bulk value in buried layers located several tens of nanometers into the film interior. From these results, it may be rationalized that the $T_{\rm g}$ nanoconfinement effect in supported PS films results from two things: (1) a significant perturbation in local segmental dynamics at the free-surface interface and (2) a mechanism by which these free-surface effects may propagate into the film interior. It is clear from ref 24 that there is not a one-to-one relationship between the length scale of a CRR at $T_{\rm g}$ and the length scale from the free surface over which $T_{\rm g}$ dynamics are modified and thus not a one-to-one relationship between the length scale of a CRR and the onset thickness at which the $T_{\rm g}$ -nanoconfinement effect is observed. However, as yet unresolved is the issue of whether there is some even qualitatively definable relationship between the length scale of a CRR at T_g in the unperturbed bulk polymer and the other two length scales. (Furthermore, a recent perspective article⁷⁷ has indicated that cooperativity length scales have been insufficiently studied in regard to their potential connection to $T_{\rm g}$ dynamics in confine-

Here we address this issue by determining the size of a single CRR at $T_{\rm g,bulk}$, $\xi_{\rm CRR}$, using the thermal fluctuation theory and DSC method by Donth. ^{47–49,78} In this approach

$$V_{\rm CRR} = \xi_{\rm CRR}^{-3} = k_{\rm B} T_{\rm g} ({\rm mid})^2 \Delta (1/C_v) / (\rho \delta T^2) \eqno(1)$$

where $V_{\rm CRR}$ is the volume of one CRR, $\xi_{\rm CRR}$ is the size (length scale) of one CRR, $k_{\rm B}$ is the Boltzmann constant, $T_{\rm g}({\rm mid})$ is the Richardson midpoint $T_{\rm g}$, $\Delta(1/C_v)$ is the step change in $1/C_v$ at the dynamic T_g , ρ is the density of bulk polymer, δT is the mean temperature fluctuation of one average CRR, and C_v is the heat capacity at constant volume. It must be noted that actual calculations employing the DSC method involve the approximation^{47,48} that $\Delta(1/C_v)$ can be replaced by $\Delta(1/C_p)$, where C_p is the heat capacity at constant pressure, a quantity that may be measured by DSC. In turn, $\Delta(1/2)$ C_p) is taken as being equivalent to $\Delta C_p/C_p^2$. (This approximation has been estimated by Donth to lead, on average, to a slight overestimation of $V_{\rm CRR}$. This is discussed further in ref 79.) The number of units present in one CRR (N_{CRR}) is given by the following:

$$N_{\rm CRR} = (\rho V_{\rm CRR} N_{\rm a}) / M_0 \tag{2}$$

where $N_{\rm a}$ is Avogadro's number and M_0 is the MW of a single repeat unit. More specific details regarding the determinations of $\xi_{\rm CRR}$ and $N_{\rm CRR}$ may be found in the Supporting Information.

Donth's approach has been described in the literature as being controversial ⁵⁶ because the associated theoretical analysis has not been verified. While acknowledging this point, we note that the experiments are straightforward and, when a reasonable temperature dependence for the cooperativity length scale is assumed, result in estimates of $\xi_{\rm CRR}$ that are consistent with the very few measurements of $\xi_{\rm CRR}$ obtained by 4D-NMR methods. For example, using eq 1 we have determined a value of ~3.3 nm⁸⁰ for $\xi_{\rm CRR}$ for glycerol at $T_{\rm g}$, allowing us to draw comparisons to results obtained for glycerol above $T_{\rm g}$ via 4D-NMR. (See Table 2 for the values of

Table 2. Sample Parameter Values Leading to the Calculation of $\xi_{\rm CRR}^{86}$ and $N_{\rm CRR}$

	A C (T/(-, TZ))	C (I/(IZ))	SZE (TZ)	TI (1) (IZ)	s d()	37 0
system	$\Delta C_p (J/(g K))$	$C_p (J/(g K))$	$\delta T\left(\mathbf{K}\right)$	$T_{\rm g}({ m mid})$ (K)	$\xi_{\mathrm{CRR}}^{d}(\mathrm{nm})$	$N_{ m CRR}^{ m e}$
PS^a	0.411	1.375	2.84	270	3.0	160
PS^b	0.277	1.873	1.90	377	3.5	255
P4MS	0.254	1.819	2.03	385	3.3	195
PTBS	0.226	2.119	2.61	405	2.6	65
$PS^c + 4 \text{ wt } \% \text{ DOP}$	0.270	1.629	2.65	362	3.0	160
glycerol	0.944	1.394	2.23	188	3.3	315

 $^aM_{\rm n}=800$ g/mol. $^bM_{\rm n}=3~000~000$ g/mol. $^cM_{\rm n}=400~000$ g/mol. d $\xi_{\rm CRR}$ values have been truncated to one digit after the decimal place. $^eN_{\rm CRR}$ values have been rounded to the nearest 5. Note: Details regarding the standard deviations associated with the parameters above may be found in the Supporting Information associated with this paper.

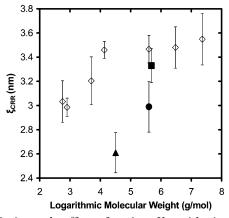


Figure 8. ξ_{CRR} values⁸⁶ as a function of logarithmic molecular weight for PS (\diamondsuit) , P4MS (\blacksquare) , PtBS (\blacktriangle) , and PS $(M_n=400\ 000\ \text{g/mol})$ doped with 4 wt % dioctyl phthalate (\bullet) . Error bars indicate the standard deviation about the mean of measured ξ_{CRR} values for that MW of PS or other polymer.

the parameters in eq 1. Also see the Supporting Information for this paper for details regarding how the values of some of the parameters were obtained.) Using 4D-NMR^{53,54} and their most recent analysis of the data, Speiss and co-workers⁸¹ report $\xi_{\rm CRR}$ values for glycerol of 1.3 ± 0.5 nm at $T_{\rm g}+10$ K, 1.1 ± 0.5 nm at $T_{\rm g}+14$ K, and 1.0 ± 0.5 nm at $T_{\rm g}+18$ K. A direct comparison of $\xi_{\rm CRR}$ values obtained by

A direct comparison of $\xi_{\rm CRR}$ values obtained by Donth's approach and 4D-NMR cannot be made at the same temperature as the former method yields data at $T_{\rm g}$ while the latter method has been applied in a certain dynamic range associated with temperatures closer to $T_{\rm g}+10$ K. Employing a dynamic scaling approach and results from dielectric spectroscopy studies by others, ^{82,83} Erwin and Colby⁵⁶ provide data indicating that $\xi_{\rm CRR}$ for glycerol increases by ~80% as temperature is decreased from $T_{\rm g}+10$ K to $T_{\rm g}$. Applying this factor to the data by Spiess and co-workers, we estimate a value of $\xi_{\rm CRR}$ of 1.44–3.24 nm for glycerol at $T_{\rm g}$. Given that there is a substantial uncertainty associated with our estimate of 3.3 nm using Donth's method (see ref 79 and further discussion below), it is possible to conclude that, when the effects of temperature difference are taken into account, determinations of $\xi_{\rm CRR}$ by 4D-NMR and Donth's approach are consistent with each other.⁸⁴

Based on our DSC measurements and eq 1, Figure 8 shows the effect of PS MW on the value of $\xi_{\rm CRR}$ over a MW range of 568–23 000 000 g/mol, an even broader MW range than employed in section A. This is also a broader MW range than that investigated 20 years ago by Donth^{49,85} in the only other study of the MW dependence of $\xi_{\rm CRR}$ for PS at $T_{\rm g}$. Figure 8 also includes the first determinations of the $\xi_{\rm CRR}$ values for P4MS, PTBS, and PS containing 4 wt % dioctyl phthalate (DOP) plasticizer. The latter system is identical to one studied in ref 25 that revealed that the $T_{\rm g}$ -nanoconfine-

ment effect can be essentially eliminated down to film thicknesses of 14 nm by diluent addition to PS. Within our range of experimental error, the size of the CRR for PS is ~ 3.5 nm, 86 invariant with MW from 23 000 000 g/mol at least down to $M_{\rm n}$ values of 13 500 g/mol. (See Table 2 for examples of parameter values that are required to determine ξ_{CRR} using eq 1.) Given the sizes of error bars in Figure 8, a case may even be made that within experimental error the size of the CRR is invariant with PS MW down to $M_{\rm n}$ values of 5000 g/mol. This value of the CRR size in PS at $T_{\rm g,bulk}$ is slightly larger than the value of 3.0 nm recently reported by Donth and co-workers⁴⁸ using regular DSC methods similar to those employed in our study. Most of this difference is due to the level of inaccuracy of the assumption that $\Delta(1/C_v) \approx \Delta(1/C_p)$, where C_p is measured by DSC. In ref 48, Donth and co-workers "correct" the $\xi_{\rm CRR}^3$ data for this inaccuracy by a common factor of 0.74⁷⁹ across all data (both low MW and polymeric glass formers). We have not made a similar adjustment to the data here in order to avoid overgeneralization, especially as we do not know the correction factor for each system employed in our study. However, we note that if we had used Donth's correction factor, it would have resulted in a value of $\xi_{CRR} = 3.1-3.2$ nm for our PS data, almost in exact agreement with Donth's value of 3.0 nm given in ref 48 (see ref 79).

In addition, the approach for determining the size of the CRR using a regular DSC method involves some "rules of thumb" for determining the δT parameter prescribed by Donth (rather than the more rigorous method by Donth involving determination of δT from the Kohlrausch-Williams-Watts exponent in conjunction with measurements by thermally modulated DSC). With the application of these rules of thumb, Donth has argued⁴⁸ that the accuracy of the characteristic size of a CRR is within 85% and 125% of the calculated value. (See Supporting Information associated with this paper for further details.) Thus, according to Donth's expectations for accuracy of the method, we can argue that for nonoligomeric PS the value of ξ_{CRR} is between 3.0 and 4.4 nm. (These values do not include Donth's factor correcting for the average inaccuracy of the assumption that $\Delta(1/C_v) = \Delta(1/C_p)$.) While this range of values for $\xi_{\rm CRR}$ may seem large, it is less than that estimated from 4D-NMR determinations of the size of a CRR for PVAc $(3.7 \pm 1 \text{ nm}).^{81}$

Figure 8 also illustrates that when the PS MW is reduced to oligomeric systems with MWs 568 or 800 g/mol, the experimentally determined $\xi_{\rm CRR}$ value is, outside of our experimental uncertainty as described by our error bars, reduced from that of our higher MW PS samples, taking on a value of \sim 3.0 nm. ⁸⁶ The fact that the size of a CRR is, within experimental error, invariant with PS MW until the MW is sufficiently reduced to yield an oligomer (or nearly an oligomer) is reason-

ably consistent with studies^{87–90} on the MW dependence of the fragility index or related behavior for PS. The fragility index m can defined by the value of d $\log(\tau)$ / $d(T_g/T)$ evaluated in the equilibrium rubbery or liquid state in the limit of $T = T_g$, where τ is the average α -relaxation time or the average relaxation time of the cooperative segmental dynamics associated with $T_{\rm g}$. 91 Often the value of m is determined at a fixed value of τ associated with $T_{\rm g}$, e.g., 100 s. The fragility index may be regarded as another measure of the nature of the cooperative motion and has been described⁸⁷ as being a "...reflection of the effect intermolecular cooperativity has on the (segmental) dynamics." A couple of studies concerning the MW dependence of the fragility index for PS have yielded the following picture: oligomeric PS (e.g., 59087 and 1100 g/mol88) exhibits a major reduction in the fragility index (or related parameters such as Ngai's coupling parameter⁸⁸) relative to high MW PS although some MW dependence to the fragility index is exhibited at MWs as high as 6400 g/mol.⁸⁷

Given the definitions of the size of an average CRR at $T_{
m g}$ and the fragility index, for a particular glassforming system both values are expected to decrease with a decrease in the number of units involved in cooperative segmental mobility at $T_{\rm g}$. In the case of PS, oligomers are expected to have a reduced requirement for cooperative segmental mobility at $T_{\rm g}$ because of the dramatically reduced connectivity between repeat units and increase in free volume that are manifested in large reductions of $T_{\rm g}$ relative to high MW PS. However, the extent to which the values of ξ_{CRR} and m are reduced with reductions in the cooperativity of a particular system may differ substantially. It has been suggested 92,93 that a value such as m reflects the apparent activation energy associated with cooperative segmental mobility in the rubbery state in the limit of $T = T_g$. This is expected to be related to the number of units involved in cooperative segmental mobility and thereby the volume of the CRR rather than the size of the CRR. Thus, m is expected to exhibit a greater change than $\xi_{\rm CRR}$ with cooperativity requirements at $T_{\rm g}$.

The experimentally measured reduction in the value of $\xi_{\rm CRR}$ from ~ 3.5 to ~ 3.0 nm^{86,94} upon addition of 4 wt % dioctyl phthalate to PS is also consistent with experimental observation of a reduction in fragility with diluent addition.88 The reduction in the size of the CRR with diluent addition is expected based on the fact that the presence of diluent reduces constraints associated with cooperative segmental motion.

In contrast to the easily explained result for diluent addition, the effect of small changes to the repeat unit structure of PS on the size of the CRR is not as easily rationalized. The value of ξ_{CRR} obtained for P4MS is \sim 3.4 nm, 86 within experimental error the same as that of PS. It is possible that the difference in repeat unit structure between PS and P4MS results in a small enough perturbation to cooperative segmental mobility that it is not evident in measurements of ξ_{CRR} . In contrast, the value of $\xi_{\rm CRR}$ obtained for PTBS is ${\sim}2.6$ nm⁸⁶ which, outside of experimental error, is even smaller than that observed for oligomeric PS. From inspection of the structures of PS and P4MS, it would be logical to assume that, other things being equal, the presence of the tert-butyl group in PTBS would greatly increase the cooperativity requirements relative to PS. However, other things are not equal in these two systems, as the 10% reduction in density of PTBS

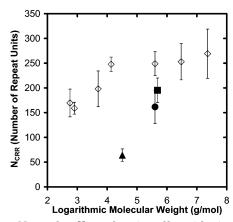


Figure 9. $N_{\rm CRR}$ values⁸⁶ as a function of logarithmic molecular weight for PS (\diamondsuit) , P4MS (\blacksquare) , PtBS (\blacktriangle) , and PS $(M_n = 400\ 000\$ g/mol) doped with 4 wt % dioctyl phthalate (●). Error bars indicate the standard deviation about the mean of measured $N_{\rm CRR}$ values for that MW of PS or other polymer.

relative to PS easily attests. Thus, the *tert*-butyl groups in PTBS greatly reduce the packing efficiency of the repeat units relative to PS, and it is surmised that this packing effect may overcome the expectation of increased cooperativity (in the absence of free volume effects) and result in a net major reduction in the size of an average cooperatively rearranging region at $T_{\rm g}$. 95 Further study of these issues in related systems is

To better appreciate the importance of packing efficiency relative to that of polymer MW in dictating the cooperativity required at T_g , Figure 9 plots the number of repeat units associated with an average CRR, $N_{\rm CRR}$, as a function of polymer MW. The value of $N_{\rm CRR}$ was calculated making the assumption that the volume of a CRR is cubic in nature (which we understand oversimplifies the shape of a CRR) and taking into account the exact density of the polymers involved; thus, the important quantitative information in Figure 9 relates to how the $N_{
m CRR}$ values depend on a particular parameter instead of the exact values of the $N_{\rm CRR}$. The oligomeric PS samples have $N_{\rm CRR}$ values that are ${\sim}60-$ 70% that of higher MW PS, in reasonable agreement with 20 year old data of Donth,49 who found a MW dependence of N_{CRR} for PS at T_{g} similar to that shown in Figure 9. (Donth actually reported MW per CRR rather than $N_{\rm CRR}$.) Most striking in Figure 9 is the fact that the PTBS sample has an $N_{\rm CRR}$ value that is 20-30% that of high MW PS. Similarly large differences among different polymers have been observed by Donth and co-workers, 48 who reported that poly(n-alkyl methacrylates) have dramatically reduced values of $N_{\rm CRR}$ relative to other polymers including PS.

We also note that two recent studies have employed the DSC method of Donth to investigate the values of $\xi_{
m CRR}$ and $N_{
m CRR}$ or $V_{
m CRR}$ for PS 50 and poly(methyl methacrylate) (PMMA)⁵¹ as a function of confinement in clay nanocomposites. Both studies reported an increase of $T_{\rm g}$ in the nanocomposite relative to neat polymer. However, the PS study reported a 75% increase in $V_{\rm CRR}$ equivalent to about a 20% increase in ξ_{CRR} , upon confinement in the nanocomposite while the PMMA study reported about a 20% decrease in ξ_{CRR} upon confinement in the nanocomposite. The different trends in these two studies suggest that at present there is not a qualitative correlation between $\xi_{\rm CRR}$ and modification of $T_{\rm g}$ in nanocomposites.

With the results provided in Figures 8 and 9, it is possible to address the issue of whether a simple qualitative relationship exists between the size of a CRR at $T_{g,\text{bulk}}$ and the T_g -nanoconfinement effect. At one level, the invariance of $\xi_{\rm CRR}$ and $N_{\rm CRR}$ with PS MW (except for oligomeric PS) is in accord with absence of a MW effect to the T_g -nanoconfinement effect in supported PS films. However, while large reductions in the values of $\xi_{\rm CRR}$ and $N_{\rm CRR}$ are observed in PTBS and PS with 4 wt % DOP relative to the values observed in neat PS, PTBS exhibits a major enhancement of the $T_{\rm g}$ -nanoconfinement effect relative to PS while the PS with 4 wt % DOP exhibits an elimination of the effect down to a film thickness of 14 nm.²⁵ Thus, the present results do not allow for a description of a "rule of thumb" regarding how a change in the size of the CRR in bulk polymer relates to the tunability of the $T_{\rm g}$ -nanoconfinement effect. However, we believe that the impact of modifications to the repeat unit structure on the nature of the polymer dynamics at the air-polymer interface as well as how such modifications impact the manner in which the perturbation to dynamics at the free surface propagate into the film interior may hold the answer. Studies of such issues as well as novel investigations to determine the general impact of interfaces on the cooperative segmental mobility (e.g., the full α -relaxation time distribution) in conjunction with repeat unit structural modifications may be key in gaining a better understanding of the $T_{\rm g}$ -nanoconfinement effect.

Conclusions

The effect of nanoconfinement on the $T_{\rm g}$ of PS films is investigated over the broadest MW range ever reported in a single study (5000-3 000 000 g/mol). In contrast to two recent reports, 20,21,69 here it is observed that PS MW has no significant impact on the film thickness dependence of $T_{\rm g}-T_{\rm g,bulk}$. This result is consistent with the substantial evidence in the literature, indicating that T_g -nanoconfinement effects originate from interfaces and surfaces which impact the cooperative segmental mobility associated with $T_{\rm g}$ and are not due to other factors which may depend on MW such as degree of chain end segregation, entanglement density, etc. In contrast, small modifications to the repeat unit structure of PS are observed to have a dramatic impact on the T_g -nanoconfinement effect. A stronger film thickness dependence of T_g is observed for P4MS compared to PS, while PTBS exhibits a stronger dependence than both PS and P4MS. The $T_{\rm g}$ reduction for a 25 nm thick PTBS film is 47 K relative to $T_{\rm g,bulk}$, which is the largest reduction from $T_{
m g,bulk}$ ever observed for supported polymer films. Furthermore, the onset thickness for the $T_{\rm g}$ -nanoconfinement effect is 300–400 nm in PTBS, the largest thickness for which such a confinement effect has been reported. These results, along with those reported in ref 25 related to the reduction or elimination of $T_{\rm g}$ -nanoconfinement effects via diluent addition, indicate that small changes in the polymer system, with the exception of MW, can yield major changes in the impact of confinement on $T_{\rm g}$ behavior.

The characteristic dynamics of the cooperative motion associated with T_g is examined via the size of a CRR at $T_{\rm g}$, $\xi_{\rm CRR}$. The value of $\xi_{\rm CRR}$ is approximately independent of PS MW over the same range of MWs for which the T_g -nanoconfinement effect is MW invariant. However, other system variations such as modification of repeat unit structure yield changes in ξ_{CRR} values of bulk polymer systems that do not correlate in an obvious manner with the strength of the T_g -nanoconfinement effect. For example, both the PS + 4 wt % DOP system and PTBS exhibit reduced values of ξ_{CRR} relative to PS; however, PS + 4 wt % DOP exhibits no T_g -nanoconfinement effect down to a film thickness of 14 nm,25 while PTBS exhibits the onset of the effect at a thickness of 300-400 nm in supported films. Future studies related to how free surfaces and interfaces impact cooperative segmental dynamics as a function of polymer repeat unit structure and diluent addition are warranted.

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Supporting Information Available: Details of the calculations of ξ_{CRR} and N_{CRR} . This material is available free of charge via the Internet at http://pubs.acs.org.

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- (85) While Donth reported in 1984 (see ref 49) on the MW dependence of the size of a CRR in PS at $T_{\rm g}$, we had a couple of reasons for believing that it was important to perform our own investigation of this issue. First, we needed to establish credibility for our experiments, which also included the effects of diluent addition to PS and modification of repeat unit structure. Second, ref 49 has been virtually forgotten in the research literature, even by Donth himself, who has not cited this reference in his later studies. This led to some concern on our part regarding the reference; those concerns were allayed by our measurements. (It should be noted that the results in ref 49 are from analysis of measurements published in: Krause, S.; Iskander, M.; Iqbal, M. Macromolecules 1982, 15, 105–111).
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(95) It is highly unlikely that the reductions in $N_{\rm CRR}$ and $\xi_{\rm CRR}$ for PTBS relative to PS have their origins in the values of the S parameter (see ref 79) for PTBS and PS. In order for the values of $N_{\rm CRR}$ and $\xi_{\rm CRR}$ to be approximately the same in the two polymers, the value of the S parameter for PTBS would need to be about 4 times that of PS.

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